## DYNAMIC MARKET MODELING WITH HETEROGENEOUS AGENTS: APPLICATIONS IN DIVERSE MARKETS

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Hidayet BEYHAN Ph. D.



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